

Section 8.1 Geometric Mean

Obj: Find geometric mean between two numbers

use geometric mean involving right triangles and their parts.

Find the mean between 12 and 18

$$12 + 18 = \frac{30}{2} = 15$$

Find the geometric mean between 12 and 18.

$$\frac{12}{x} = \frac{x}{18}$$

$$\sqrt{x^2} = \sqrt{216}$$

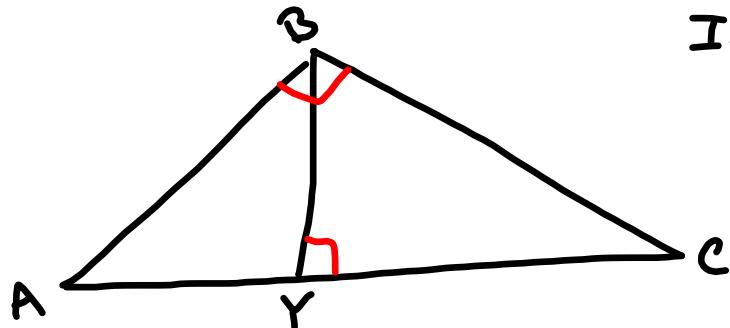
$$x = 14.70$$

$$\frac{12}{14.70} \approx .82$$

$$\frac{14.70}{18} \approx .82$$

Find the geometric mean between 9 and 37.

$$18.25$$

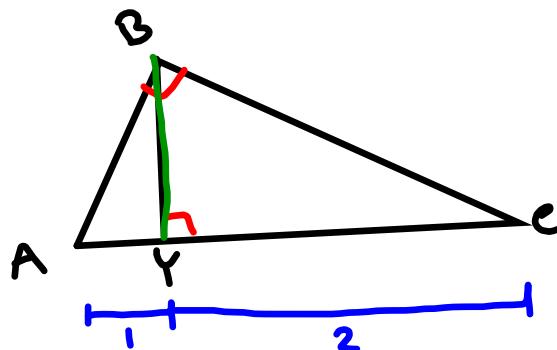


If an altitude is drawn to the hypotenuse of a right triangle, then the original triangle is divided into two similar triangles which are similar to the original.

$$\triangle ABY \sim \triangle BCY$$

$$\triangle ABY \sim \triangle ACB$$

$$\triangle BCY \sim \triangle ACB$$



If an altitude is drawn to the hypotenuse of a right, then the altitude is the geometric mean between the two segments of the hypotenuse.

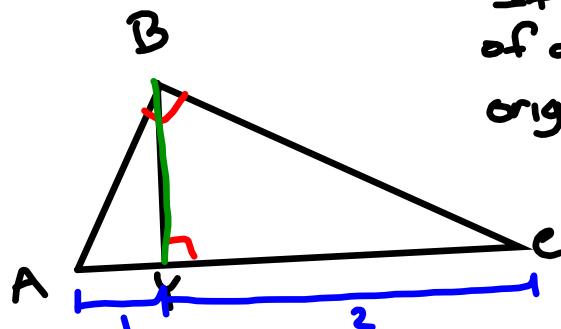
$$\frac{AY}{BY} = \frac{BY}{YC}$$

$$BY = 10, YC = 20, \text{Find } AY$$

$$\frac{x}{10} = \frac{10}{20} \quad 20x = 100 \\ x = 5$$

$$AC = 25, AY = 8, \text{Find } BY$$

$$\frac{8}{x} = \frac{x}{17} \quad x = 11.66$$



If an altitude is drawn to the hypotenuse of a right triangle, then either leg of the original triangle is the geometric mean between the original hypotenuse and the segment of the hypotenuse adjacent to the original leg.

$$\text{If } \overline{AB}$$

$$\frac{AC}{AB} = \frac{AB}{AY}$$

$$\text{If } \overline{BC}$$

$$\frac{AC}{BC} \neq \frac{BC}{YC}$$

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